

## Electronic Supplementary Information

# Phase equilibria in the CeO<sub>2</sub>–La<sub>2</sub>O<sub>3</sub>–Gd<sub>2</sub>O<sub>3</sub> system at 1250 and 1500 °C

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**Table S1.** Phase composition and lattice parameters of the phases in the La<sub>2</sub>O<sub>3</sub>–Gd<sub>2</sub>O<sub>3</sub> system, annealed at 1600 °C for 10 h in air (according to XRD)

Chemical composition (mol %)		Phase composition	Lattice parameters of the phases (nm)							
			<A>* La <sub>2</sub> O <sub>3</sub> Gd <sub>2</sub> O <sub>3</sub>			<B> <i>a</i> <i>b</i> <i>c</i> $\beta$				
<i>a</i>	<i>c</i>	<i>c/a</i>	<i>a</i>	<i>b</i>	<i>c</i>	$\beta$				
100	0	<A>*	0.6523	0.3855	0,5909	–	–	–	–	–
95	5	<A>*	0.6517	0.3837	0.5887	–	–	–	–	–
90	10	<A>*	0.6496	0.3817	0.5876	–	–	–	–	–
85	15	<A>*	0.6491	0.3809	0.5868	–	–	–	–	–
80	20	<A>*	0.6478	0.3797	0.5861	–	–	–	–	–
75	25	<A>*	0.6468	0.3750	0.5798	–	–	–	–	–
65	35	<A>*	0.6458	0.3737	0.5787	–	–	–	–	–
60	40	<A>*+<B>	0.6447	0.3716	0.5764	1.4726	0.3632	0.9068	88.96	
55	45	<A>*+<B>	0.6449	0.3710	0.5753	1.4721	0.3641	0.9052	92.46	
50	50	<A>*+<B>	0.6446	0.3712	0.5758	1.4695	0.3634	0.9011	92.41	
45	55	<A>*+<B>	0.6448	0.3718	0.5766	1.4671	0.3621	0.9000	92.47	
40	60	<A>*+<B>	–	–	–	1.4597	0.3611	0.8968	92.55	
35	65	<A>*+<B>	–	–	–	1.4573	0.3597	0.8952	92.40	
30	70	<B>	–	–	–	1.4579	0.3577	0.8925	92.05	
25	75	<B>	–	–	–	1.4540	0.3579	0.8914	92.50	
20	80	<B>	–	–	–	1.4514	0.3573	0.8882	92.53	

15	85	<B>	—	—	—	1.4543	0.3563	0.8800	92.64
10	90	<B>	—	—	—	1.4446	0.3557	0.8905	92.28
5	95	<B>	—	—	—	1.4394	0.3549	0.8800	92.73
0	100	<B>	—	—	—	1.4341	0.3566	0.8773	93.25

At given conditions ( at 1600°C for 10 h in air) the hexagonal modification of A-La<sub>2</sub>O<sub>3</sub> unquenchable and hexagonal modification of La(OH)<sub>3</sub> was observed instead. Designation of phases: <A\*>, solid solutions based on hexagonal modification of La<sub>2</sub>O<sub>3</sub>; <B>, solid solutions based on monoclinic modification of Gd<sub>2</sub>O<sub>3</sub>

**Table S2.** Phase composition and lattice parameters of the phases in the La<sub>2</sub>O<sub>3</sub>–Gd<sub>2</sub>O<sub>3</sub> system, annealed at 1500 °C for 225 h in air (according to XRD)

Chemical composition (mol %)		Phase composition	Lattice parameters of the phases (nm)							
			<A*>			<B>				
La <sub>2</sub> O <sub>3</sub>	Gd <sub>2</sub> O <sub>3</sub>		<i>a</i>	<i>c</i>	<i>c/a</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>β</i>	
100	0	<A*>	0.6523	0.3855	0.5909	—	—	—	—	
95	5	<A*>	0.6494	0.3818	0.5879	—	—	—	—	
90	10	<A*>	0.6491	0.3818	0.5882	—	—	—	—	
85	15	<A*>	0.6481	0.3841	0.5926	—	—	—	—	
80	20	<A*>	0.6479	0.3797	0.5860	—	—	—	—	
75	25	<A*>	0.6468	0.3781	0.5846	—	—	—	—	
70	30	<A*>	0.6470	0.3777	0.5838	—	—	—	—	
65	35	<A*> + <B>	0.6461	0.3747	0.5799	—	—	—	—	
60	40	<A*> + <B>	0.6464	0.3749	0.5799	1.3635	0.3562	0.8896	90.36	
55	45	<A*> + <B>	0.6460	0.3736	0.5783	1.4283	0.3556	0.8865	87.19	
50	50	<A*> + <B>	0.6458	0.3746	0.5800	1.4221	0.3542	0.8856	87.85	
45	55	<A*> + <B>	0.6467	0.3746	0.5792	1.4198	0.3523	0.8826	87.55	
40	60	<A*> + <B>	0.6471	0.3749	0.5794	1.44642	0.3656	0.8752	91.44	
35	65	<B>	—	—	—	1.4588	0.3643	0.8973	91.44	
30	70	<B>	—	—	—	1.4567	0.3635	0.8954	91.51	
25	75	<B>	—	—	—	1.4540	0.3621	0.8926	91.22	

20	80	<B>	-	-	-	1.4492	0.3610	0.8907	91.61
10	90	<B>	-	-	-	1.3907	0.3591	0.8818	87.38
0	100	<B>	-	-	-	1.4335	0.3566	0.8813	91.85

\* At given conditions (at 1600°C for 10 h in air) the hexagonal modification of A-La<sub>2</sub>O<sub>3</sub> unquenchable and hexagonal modification of La(OH)<sub>3</sub> was observed instead. Designation of phases: <A\*>, solid solutions based on hexagonal modification of La<sub>2</sub>O<sub>3</sub>; <B>, solid solutions based on monoclinic modification of Gd<sub>2</sub>O<sub>3</sub>;

**Table S3.** Phase composition and lattice parameters of the phases in the La<sub>2</sub>O<sub>3</sub>–Gd<sub>2</sub>O<sub>3</sub> system, annealed at 1100 °C for 9820 h in air (according to XRD)

Chemical composition (mol %)		Phase composition	Lattice parameters of the phases (nm)								
La <sub>2</sub> O <sub>3</sub>	Gd <sub>2</sub> O <sub>3</sub>		<A*>				<B>				
			<i>a</i>	<i>c</i>	<i>c/a</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>β</i>		
100	0	<A*>	0.6523	0.3855	0.5909	-	-	-	-	-	
95	5	<A*>	0.6497	0.3835	0.5903	-	-	-	-	-	
90	10	<A*>	0.6492	0.3825	0.5892	-	-	-	-	-	
85	15	<A*>	0.6489	0.3815	0.5879	-	-	-	-	-	
80	20	<A*> + <B>	0.6494	0.3797	0.5854	-	-	-	-	-	
75	25	<A*> + <B>	0.6497	0.3788	0.5837	1.4331	0.5119	0.8581	115.57		
70	30	<A*> + <B>	0.6477	0.3781	0.5838	1.6157	0.6423	0.8653	126.97		
65	35	<A*> + <B>	0.6488	0.3808	0.5884	1.6675	0.6784	0.8644	129.37		
60	40	<B>	-	-	-	1.4704	0.3548	0.9137	88.96		
55	45	<B>	-	-	-	1.4672	0.3627	0.9076	90.58		
45	55	<B>	-	-	-	-	-	-	-		
40	60	<B>	-	-	-	1.4052	0.3651	0.8946	87.18		
35	65	<B>	-	-	-	1.4077	0.3644	0.8944	87.49		
30	70	<B>	-	-	-	1.3986	0.3627	0.8892	87.66		
25	75	<B>	-	-	-	1.3981	0.3619	0.8870	87.72		
20	80	<B> + <C>	-	-	-	1.3940	0.3606	0.8844	87.45		
15	85	<B> + <C>	-	-	-	1.3919	0.3598	0.8827	87.48		
10	90	<B> + <C>	-	-	-	1.3907	0.3591	0.8818	87.38		

5	95	$\langle B \rangle + \langle C \rangle$ $a = 1.0816$	-	-	-	1.4340	0.3430	0.8926	88.82
0	100	$\langle C \rangle$ $a = 1.0777$	-	-	-	-	-	-	-

At given conditions (at 1600°C for 10 h in air) the hexagonal modification of A-La<sub>2</sub>O<sub>3</sub> unquenchable and hexagonal modification of La(OH)<sub>3</sub> was observed instead. Designation of phases: <A\*>, solid solutions based on hexagonal modification of La<sub>2</sub>O<sub>3</sub>; <B>, solid solutions based on monoclinic modification of Gd<sub>2</sub>O<sub>3</sub> <C>, solid solutions based on cubic modification of Gd<sub>2</sub>O<sub>3</sub>

**Table S4** Phase composition and lattice parameters of CeO<sub>2</sub>–La<sub>2</sub>O<sub>3</sub>–Gd<sub>2</sub>O<sub>3</sub> samples annealed at 1500 °C for 130 h (according to XRD and scanning electron microscopy)

Chemical composition, mol%			Phase composition and lattice parameters of the phases a (nm) by XRD data	Lattice parameter of phases, nm	
CeO <sub>2</sub>	La <sub>2</sub> O <sub>3</sub>	Gd <sub>2</sub> O <sub>3</sub>		<C>	<F>
1	2	3	4	5	6
Section CeO <sub>2</sub> – (50 mol % La <sub>2</sub> O <sub>3</sub> – 50 mol % Gd <sub>2</sub> O <sub>3</sub> )					
5	47.5	47.5	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6395, c = 0.3744$ )	-	0.5516
10	45	45	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6444, c = 0.3708$ )	-	0.5515
15	42.5	42.5	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6437, c = 0.3699$ )	-	0.5514
20	40	40	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6419, c = 0.3710$ )	-	0.5509
25	37.5	37.5	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$	-	0.5516
30	35	35	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$	-	0.5516
35	32.5	32.5	$\langle F \rangle + \langle B \rangle$	-	0.5512
40	30	30	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1020	0.5510
45	27.5	27.5	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1019	0.5509
50	25	25	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1021	0.5510
55	22.5	22.5	$\langle F \rangle + \langle C \rangle$	1.0998	0.5508
60	20	20	$\langle F \rangle + \langle C \rangle$	1.0992	0.5504
65	17.5	17.5	$\langle F \rangle$	-	0.5493
70	15	15	$\langle F \rangle$	-	0.5483
75	12.5	12.5	$\langle F \rangle$	-	0.5477
80	10	10	$\langle F \rangle$	-	0.5466
85	7.5	7.5	$\langle F \rangle$	-	0.5451
90	5	5	$\langle F \rangle$	-	0.5439
95	2.5	2.5	$\langle F \rangle$	-	0.5425
100	0	0	$\langle F \rangle$	-	0.5409
Section La <sub>2</sub> O <sub>3</sub> – (50 mol % CeO <sub>2</sub> – mol % Gd <sub>2</sub> O <sub>3</sub> )					
50	0	50	$\langle F \rangle + \langle C \rangle$	1.0836	0.5418
47.5	5	47.5	$\langle F \rangle + \langle C \rangle$	1.0868	0.5434
45	10	45	$\langle F \rangle + \langle C \rangle$	1.0888	0.5446
42.5	15	42.5	$\langle F \rangle + \langle C \rangle$	1.0930	0.5465

40	20	40	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.0960	0.5478
35	30	35	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.0959	0.5479

Table 4 Continued

1	2	3	4	5	6
32.5	35	32.5	$\langle F \rangle + \langle B \rangle$	—	0.5502
30	40	30	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6432, c = 0.3769$ )	—	0.5526
27.5	45	27.5	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6438, c = 0.3768$ )	—	0.5526
25	50	25	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6469, c = 0.3759$ )	—	0.5531
22.5	55	22.5	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6473, c = 0.3784$ )	—	0.5528
20	60	20	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$ ( $a = 0.6499, c = 0.3775$ )	—	0.5525
17.5	65	17.5	$\langle F \rangle + \langle A^* \rangle$ ( $a = 0.6493, c = 0.3775$ )	—	0.5546
12.5	75	12.5	$\langle F \rangle + \langle A^* \rangle$ ( $a = 0.6493, c = 0.3775$ )	—	0.5556
10	80	10	$\langle F \rangle + \langle A^* \rangle$ ( $a = 0.6524, c = 0.3810$ )	—	0.5571
7.5	85	7.5	$\langle F \rangle + \langle A^* \rangle$ ( $a = 0.6524, c = 0.3810$ )	—	0.5579
5	90	5	$\langle A^* \rangle$ ( $a = 0.6534, c = 0.3820$ )	—	—
2.5	95	2.5	$\langle A^* \rangle$ ( $a = 0.6536, c = 0.3822$ )	—	—
Iso-concentration line 15 mol % CeO <sub>2</sub>					
15	10	75	$\langle C \rangle + \langle B \rangle$	1.0865	—
15	15	70	$\langle C \rangle + \langle B \rangle$	1.0891	—
15	20	65	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.0915	0.5482
15	25	60	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.0918	0.5480
15	30	55	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.0912	0.5481
15	35	50	$\langle F \rangle + \langle B \rangle$	—	0.5488
15	40	45	$\langle F \rangle + \langle A^* \rangle + \langle B \rangle$	—	0.5494
15	45	40	$\langle F \rangle + \langle A^* \rangle + \langle B \rangle$	—	0.5498
15	50	35	$\langle F \rangle + \langle A^* \rangle + \langle B \rangle$	—	0.5493
15	55	30	$\langle F \rangle + \langle A^* \rangle + \langle B \rangle$ ( $a = 0.6524, c = 0.3810$ )	—	0.5498
15	60	25	$\langle F \rangle + \langle A^* \rangle + \langle B \rangle$ ( $a = 0.6456, c = 0.3773$ )	—	0.5500
15	65	20	$\langle F \rangle + \langle A^* \rangle + \langle B \rangle$ ( $a = 0.6477, c = 0.3781$ )	—	0.5496

15	70	15	$\langle A^* \rangle + \langle F \rangle$ ( $a = 0.6477, c = 0.3802$ )	-	0.5505
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Table 4 Continued

1	2	3	4	5	6
15	75	10	$\langle A^* \rangle + \langle F \rangle$ ( $a = 0.6506, c = 0.3799$ )	-	0.5510
15	80	5	$\langle A^* \rangle + \langle F \rangle$ ( $a = 0.6525, c = 0.3799$ )	-	0.5516
Iso-concentration line 45 mol % CeO <sub>2</sub>					
45	5	50	$\langle F \rangle + \langle C \rangle$	1.0868	0.5434
45	10	45	$\langle F \rangle + \langle C \rangle$	1.0902	0.5451
45	15	40	$\langle F \rangle + \langle C \rangle$	1.0938	0.5469
45	25	30	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.1159	0.5499
45	30	25	$\langle F \rangle + \langle C \rangle + \langle B \rangle$	1.1057	0.5494
45	35	20	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$	-	0.5532
45	40	15	$\langle F \rangle + \langle B \rangle + \langle A^* \rangle$	-	0.5535
45	45	10	$\langle F \rangle + \langle A^* \rangle$	-	0.5563

\*At given conditions (at 1500°C for 130 h in air) the hexagonal modification of A-La<sub>2</sub>O<sub>3</sub> unquenchable and hexagonal modification of La(OH)<sub>3</sub> was observed instead. Designation of phases:  $\langle A^* \rangle$ , solid solutions based on hexagonal modification of La<sub>2</sub>O<sub>3</sub>;  $\langle F \rangle$ , solid solutions based on cubic modification with fluorite-type structure of CeO<sub>2</sub>;  $\langle C \rangle$ , solid solutions based on cubic modification of Gd<sub>2</sub>O<sub>3</sub>;  $\langle B \rangle$ , solid solutions based on monoclinic modification of Gd<sub>2</sub>O<sub>3</sub>

**Table S5** – Phase composition and lattice parameters of CeO<sub>2</sub>–La<sub>2</sub>O<sub>3</sub>–Gd<sub>2</sub>O<sub>3</sub> samples annealed at 1250 °C for 6200 h (according to XRD)

Chemical composition, mol%			Phase composition and lattice parameters of the phases a (nm) by XRD data	Lattice parameter of phases, nm	
				<C>	<F>
1	2	3		4	5
Section CeO <sub>2</sub> –(50 mol % La <sub>2</sub> O <sub>3</sub> –50 mol % Gd <sub>2</sub> O <sub>3</sub> )					
5	47.5	47.5	$\langle F \rangle + \langle A \rangle + \langle B \rangle$	-	0.5545
10	45	45	$\langle F \rangle + \langle B \rangle$	-	0.5542
15	42.5	42.5	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1071	0.5534
20	40	40	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1073	0.5536
25	37.5	37.5	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1070	0.5538
30	35	35	$\langle F \rangle + \langle B \rangle + \langle C \rangle$	1.1066	0.5533

35	32.5	32.5	<F>+<B>+<C>	1.1074	0.5537
40	30	30	<F>+<B>+<C>	1.1071	0.5536
45	27.5	27.5	<F>+<C>	1.1062	0.5531
50	25	25	<F>+<C>	1.1058	0.5527
55	22.5	22.5	<F>+<C>	1.1055	0.5516
60	20	20	<F>	—	0.5498
65	17.5	17.5	<F>	—	0.5493
70	15	15	<F>	—	0.5481
75	12.5	12.5	<F>	—	0.5470
80	10	10	<F>	—	0.5450
85	7.5	7.5	<F>	—	0.5446
90	5	5	<F>	—	0.5436
95	2.5	2.5	<F>	—	0.5419
100	0	0	<F>	—	0.5409
Section La <sub>2</sub> O <sub>3</sub> –(50 mol % CeO <sub>2</sub> –50 mol % Gd <sub>2</sub> O <sub>3</sub> )					
50	0	50	<F> + <C>	1.0865	0.5433
47.5	5	47.5	<F> + <C>	1.0869	0.5435
45	10	45	<F> + <C>	1.0898	0.5449
42.5	15	42.5	<F> + <C>	1.0936	0.5467
40	20	40	<F> + <C>	1.0999	0.5499
37.5	25	37.5	<F> + <C> + <B>	1.1039	0.5520

Table 5 Continued

1	2	3	4	5	6
35	30	35	<F> + <C> + <B>	1.1040	0.5515
32.5	35	32.5	<F> + <C> + <B>	1.1038	0.5522
30	40	30	<F> + <C> + <B>	1.1037	0.5518
27.5	45	27.5	<F> + <B>	—	0.5528
25	50	25	<F>+<B>+<A*> <i>(a = 0.6471, c = 0.3782)</i>	—	0.5536
20	60	20	<F>+<B>+<A*> <i>(a = 0.6473, c = 0.3784)</i>	—	0.5535
15	70	15	<F>+<B>+<A*> <i>(a = 0.6475, c = 0.3786)</i>	—	0.5537
10	80	10	<F>+<B>+<A*> <i>(a = 0.6473, c = 0.3784)</i>	—	0.5536
7.5	85	7.5	<F>+<A*> <i>(a = 0.6524, c = 0.3810)</i>	—	0.5542
5	90	5	<A*> <i>(a = 0.6534, c = 0.3820)</i>	—	—

2.5	95	2.5	$\langle A^* \rangle \quad a = 0.6536, c = 0.3822$	—	—
Iso-concentration line 15 mol % CeO <sub>2</sub>					
15	0	85	<C>	1.0830	—
15	5	80	<C>	1.0838	—
15	10	75	< C > + < B >	1.0850	—
15	15	70	< C > + < B >	1.0872	—
15	20	65	< F >+< C > + < B >	1.0891	0.5520
15	25	60	< F >+< C > + < B >	1.0892	0.5522
15	30	55	< F >+< C > + < B >	1.0899	0.5518
15	35	50	< F >+< C > + < B >	1.0910	0.5521
15	40	45	< F >+< C > + < B >	1.0898	0.5520
15	45	40	< F >+ < B >	—	0.5530
15	50	35	< F >+< B > + < A > ( $a = 0.6477, c = 0.3781$ )	—	0.5535
15	60	25	< F >+< B > + < A > ( $a = 0.6477, c = 0.3802$ )	—	0.5537
15	75	10	< F >+< B > + < A > ( $a = 0.6479, c = 0.3800$ )	—	0.5534
15	80	5	< F > + < A > ( $a = 0.6523, c = 0.3797$ )	—	0.5540

\*At given conditions ( at 1250°C for 620 h in air) the hexagonal modification of A-La<sub>2</sub>O<sub>3</sub> unquenchable and hexagonal modification of La(OH)<sub>3</sub> was observed instead. Designation of phases: <A\*>, solid solutions based on hexagonal modification of La<sub>2</sub>O<sub>3</sub>; <F>, solid solutions based on cubic modification with fluorite-type structure of CeO<sub>2</sub>; <C>, solid solutions based on cubic modification of Gd<sub>2</sub>O<sub>3</sub>; <B>, solid solutions based on monoclinic modification of Gd<sub>2</sub>O<sub>3</sub>